



**ALL SAINTS'
COLLEGE**

WA Exams Practice Paper D, 2016

Question/Answer Booklet

**MATHEMATICS
SPECIALIST
UNIT 3**

**Section One:
Calculator-free**

If required by your examination administrator, please
place your student identification label in this box

Student Number: In figures

--	--	--	--	--	--	--	--

In words

Your name

Time allowed for this section

Reading time before commencing work: five minutes

Working time for section: fifty minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer Booklet

Formula Sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	7	7	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
Total				150	100

Instructions to candidates

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer Booklet.
3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.
5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

Section One: Calculator-free

35% (52 Marks)

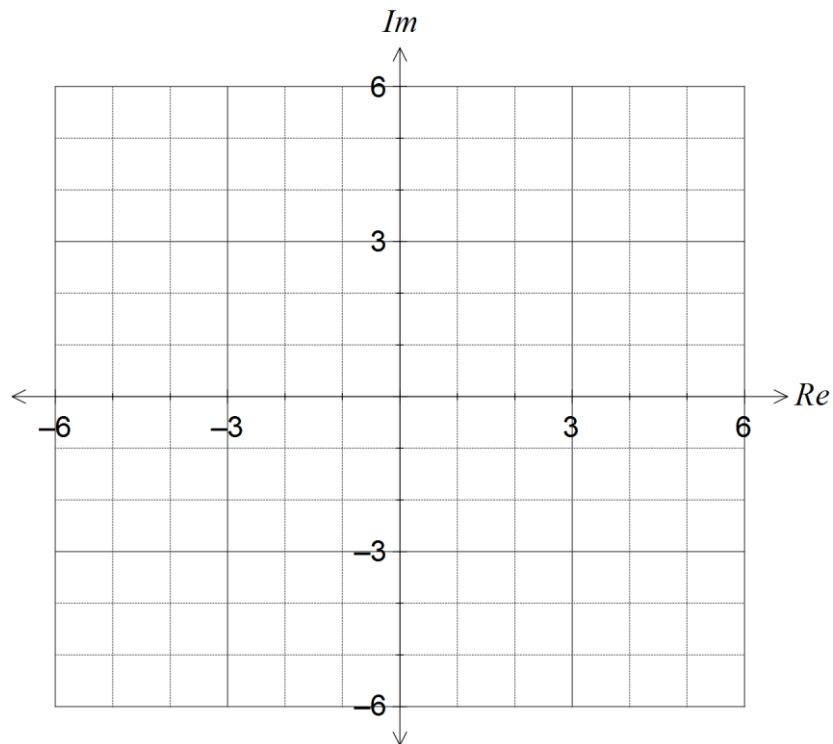
This section has **seven (7)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time for this section is 50 minutes.

Question 1

(5 marks)

- (a) Plot and label the complex numbers $w = 2 + i$ and $z = -1 - 2i$ on the Argand diagram below. (1 mark)



- (b) On the same diagram plot and label the following complex numbers:

- (i) $z_1 = i^3 z$. (1 mark)
- (ii) $z_2 = 3w + 2z$. (1 mark)
- (iii) $z_3 = wz$. (1 mark)
- (iv) $z_4 = \frac{5}{w}$. (1 mark)

Question 2**(7 marks)**

Consider the following system of equations:

$$x + 2y + 2z = 4$$

$$2x + y + 3z = 6$$

$$x + y + az = a - 1$$

(a) Solve the system of equations when $a = 3$.

(3 marks)

(b) Determine the value of a for which the system has no solution.

(4 marks)

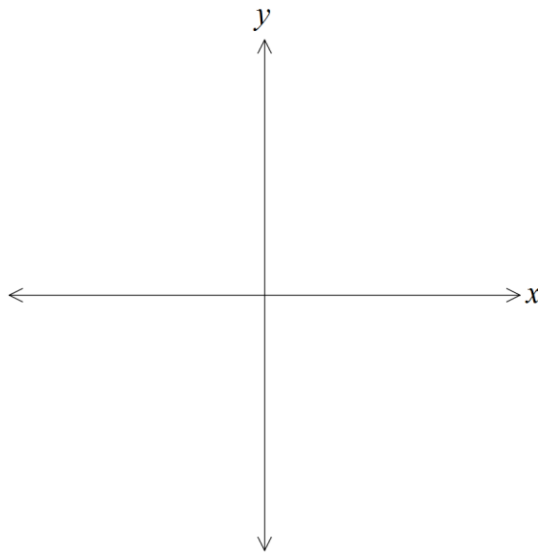
Question 3

(7 marks)

Two functions are defined by $f(x) = x^2 + 2$ and $g(x) = \sqrt{1 - x^2}$ for real numbers over their natural domains.

(a) Calculate $f \circ g(0)$. (1 mark)

(b) Sketch the graph of the composite function $y = f \circ g$ on the axes below. (3 marks)



(c) State a domain restriction for f so that it becomes a one-to-one function with the largest possible range. (1 mark)

(d) Explain, with reasons, whether the composite function $g \circ f$ is a valid function. (2 marks)

Question 4

(7 marks)

(a) Given that $z = 1 + i$,(i) express z in polar form.

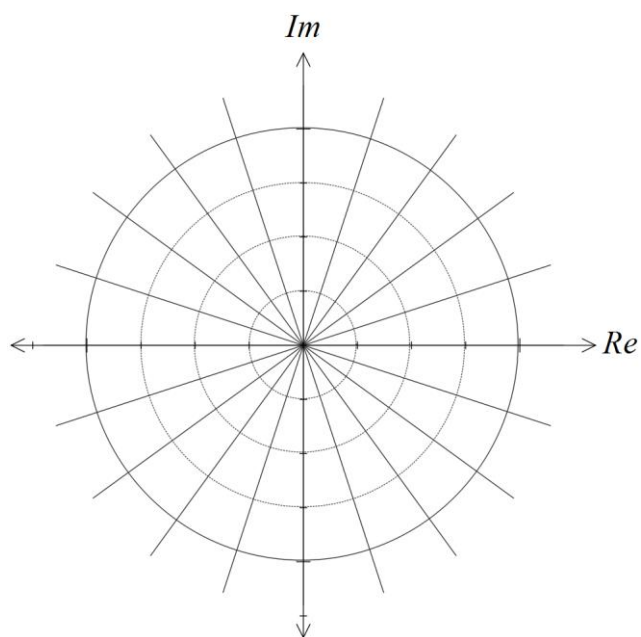
(1 mark)

(ii) Determine $\left(\frac{1}{z}\right)^6$

(3 marks)

(b) If $z^5 = 1$, sketch the location of the five roots of this equation on the axes below.

(3 marks)



See next page

Question 5

(8 marks)

- (a) Determine the remainder when the polynomial $z^2 + z - 1 + 2i$ is divided by $z - 1 - i$.
(2 marks)

- (b) Consider $h(z) = z^4 - 4z^3 + 4z^2 + 4z - 5$, $z \in \mathbb{C}$. Solve $h(z) = 0$ over \mathbb{C} . (6 marks)

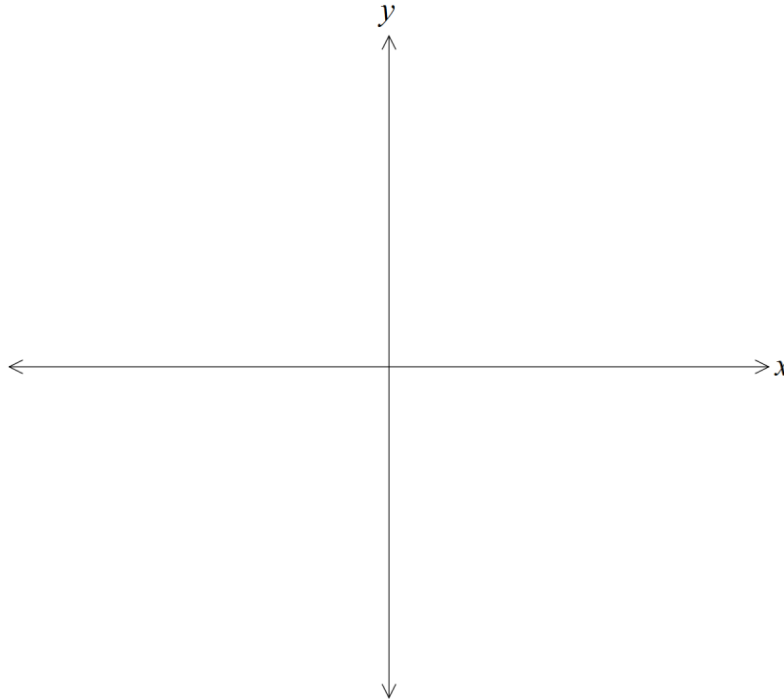
Question 6

(9 marks)

A function is defined by $f(x) = \frac{x-1}{2x+2}$.

(a) Sketch the graph of $y = f(x)$ on the axes below.

(4 marks)



(b) Determine the equation of the inverse function, $f^{-1}(x)$.

(3 marks)

(c) State the equations of all asymptotes of the graph of $y = f^{-1}(x)$.

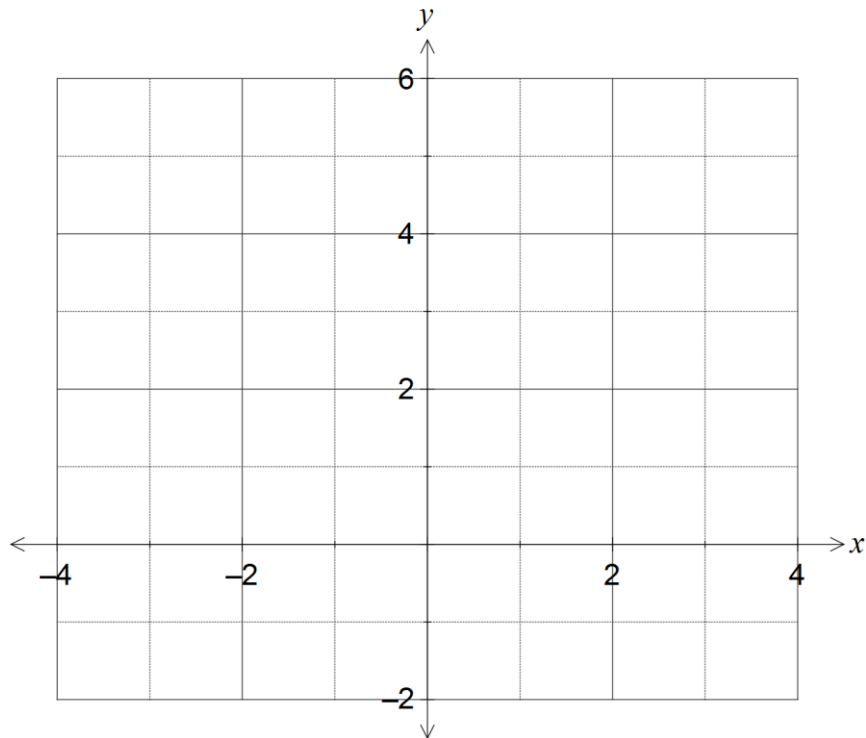
(2 marks)

Question 7

(9 marks)

(a) Sketch the graph of $y = |x - 1| + \left| \frac{x}{2} + 1 \right|$.

(4 marks)



(b) The solution to the equation $a|x + b| + c = |x - 1| + \left| \frac{x}{2} + 1 \right|$ is $\{x : -1 \leq x \leq 1\}$.

(i) Sketch a possible graph of $y = a|x + b| + c$ on the axes above. (2 marks)

(ii) Determine the values of the real constants a , b and c . (3 marks)

Additional working space

Question number: _____

Additional working space

Question number: _____

© 2015 WA Exam Papers. All Saints' College has a non-exclusive licence to copy and communicate this paper for non-commercial, educational use within the school. No other copying, communication or use is permitted without the express written permission of WA Exam Papers.